Seat No.

Set: A

B.C.A. (Part-I) (Semester-II) (CBCS/NEP)

Examination Oct./Nov 2023.

College Name: Kamala College, Kolhapur

Subject Name: Mathematical Foundations For Computer Applications

Subject Code: 80872

Total Marks: 70

Day and Date: Friday 03/11/2023

Period: 3 hours

Time: 12.00 p.m. to 03.00 p.m.

Total Pages: 04

Instructions:

1) Oue 1 and Que 6 are compulsory.

2) Attempt any three questions from que No 2 to que No 5

3) Figure to the eight indicate marks.

Q.1 A] Select the correct alternative for each of the following [10]

- 1) Given that the set, $A = \{1, 2, 3\}$, $B = \{3, 4\}$, $C = \{4, 5, 6\}$ then $A \cup (B \cap C)$ is:

- a) {3} b) {1, 2, 3,4} c) {1, 2, 5, 6} d) {1, 2, 3, 4, 5, 6}

2) The dual of $(\sim p \land q) \lor (p \land t)$

- a) $(p \land q) \lor (p \land c)$ b) $(\sim p \lor \sim q) \land (\sim p \lor c)$
- c) $(\sim p \vee q) \wedge (p \vee c)$ d) $(\sim p \vee q) \wedge (p \vee t)$

3) If $A = \begin{bmatrix} 1 & 5 & -7 \\ 2 & 6 & 8 \end{bmatrix}$ then $A^{T} = \dots$

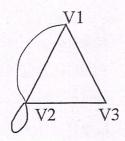
a)
$$\begin{pmatrix} 2 & 6 & 8 \\ 1 & 5 & -7 \end{pmatrix}$$
 b) $\begin{pmatrix} 5 & 1 & -7 \\ 6 & 2 & 8 \end{pmatrix}$ c) $\begin{pmatrix} 1 & 2 \\ 5 & 6 \\ -7 & 8 \end{pmatrix}$ d) $\begin{pmatrix} 2 & 1 \\ 6 & 5 \\ 8 & -7 \end{pmatrix}$

b)
$$\begin{bmatrix} 5 & 1 & -7 \\ 6 & 2 & 8 \end{bmatrix}$$

c)
$$\begin{pmatrix} 1 & 2 \\ 5 & 6 \\ -7 & 8 \end{pmatrix}$$

d)
$$\begin{pmatrix} 2 & 1 \\ 6 & 5 \\ 8 & -7 \end{pmatrix}$$

- 4) The degree of vertex V_2 in the adjoining multigraph is....
 - a) 5
- b) 4
- c) 3
- d) 6



- 5) If A and B are two sets such that n(A) = 50, n(B) = 30, $n(A \cup B) = 60$ then n (A \cap B) is equal to...
 - a) 140
- b) 50
- c) 20
- d) 30
- 6) Which of the following sentence is not a statement?
 - a) 8 has 4 divisors
- b) Read the book
- c) 8 + 9 = 17
- d) Square of an odd number is even
- 7) The Value of $\begin{vmatrix} 1 & 0 & 2 \\ 2 & 1 & 1 \\ 1 & 2 & 3 \end{vmatrix}$ is b) 7 c) 9 a) 1



- 8) The number of vertices in Km, n is...
 - a) m + n
- b) $m^2 + n^2$
- c) mn
- d) m-n
- 9) The power set of the set {O} is.....

- b) {O} c) {Ø} d) {Ø, {O}}
- 10) The converse of $p \rightarrow q$ is
- a) $q \to p$ b) $\sim p \to q$ c) $\sim q \to \sim p$ d) $\sim p \to \sim q$

i) Let
$$A = \{1, 2, 3, 4\}, B = \{4,5,6\}, C = \{5, 6\}$$
 find,

i)
$$A \times (B \cap C)$$
 ii) $(A \times B) \cap (A \times C)$

ii) Define 'Graph' with example And Explain Walk, Path, cycle

iii) If
$$A = \begin{bmatrix} 7 & 3 \\ 3 & 5 \end{bmatrix}$$
 and $B = \begin{bmatrix} -5 & 3 \\ 3 & -7 \end{bmatrix}$

Find |A| and |B|, and show that AB is a non - singular matrix

Q.2) a) Define the term "statement" And write the converse, inverse and contrapositive of

"If you are good in logic, then you are good in Mathematics"

- b) Define the term 'Tautology' And check whether the following statement pattern is a Tautology, Contradiction or contingency $[(p \rightarrow q) \land q] \rightarrow p$ [5+5]
- LIBP LIBP Q. 3) a) There are 260 persons with a Skin disorder. If 150 had been exposed to the chemical A, 74 to the chemical B and 36 to both chemical A and B, find the number of persons exposed to
- i) Chemical A but not chemical B
- ii) Chemical A or chemical B
- b) Define finite set And solve

If $A = \{1, 2, 3, 4\}$, $B = \{3, 4, 5, 6\}$ $C = \{4, 5, 6, 7, 8\}$ and universal set

$$X = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$$
 then verify that,

i)
$$A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$$

ii)
$$(A \cup B)' = A' \cap B'$$

[5 + 5]

- Q 4) a) Define Degree of vertex, and hence explain even vertex, odd vertex, Isolated vertex and pendant vertex.
 - b) Define digraph and also explain walk, path, cycle

[5 + 5]

Q 5) a) Define transpose of a matrix.

If
$$A = \begin{bmatrix} 1 & 2 \\ 3 & 5 \end{bmatrix}$$
, $B = \begin{bmatrix} 0 & 4 \\ 2 & -1 \end{bmatrix}$ then show that $AB \neq BA$

b) Define Scalar matrix. Apply elementary transformation for,

$$A = \begin{bmatrix} 1 & 2 & -1 \\ 0 & 1 & 3 \end{bmatrix}$$
, $2C_2$ and $B = \begin{bmatrix} 1 & 0 & 2 \\ 2 & 4 & 4 \end{bmatrix}$, $-3R_1$

Find the addition of two new matrices

$$[5 + 5]$$

Q. 6) Write short note on the following [Any Four out of six]

[20]

- i) Operations on set
- ii) Adjacency and Incidence matrix
- iii) Diagonal matrix, singular matrix, Identity matrix
- iv) Conjunction, disjunction, negation
- v) Types of Functions
- vi) Simple graph, complete graph, regular graph.

